Peculiar pressure effect on Poisson ratio of graphene as a strain damper†
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Hydrogenation is an effective way to modify the electronic and magnetic properties of graphene. The semi-hydrogenated graphene, known as “graphone”, has promising applications in nanoelectronics including field-effect transistors. However, the elastic limit of this two-dimensional material remains unknown despite its importance in applications as well as strain engineering to tailor functions and properties. Here we report using first-principles calculations an abnormal increase in the Poisson ratio of graphene in response to an increase in pressure. This peculiar behavior is proposed to originate from the asymmetry of hydrogenation and could be used to design a nanodevice of strain damper to reduce harmful strains in graphene-based nanoelectronics.

Graphene is a derivative of graphene with only one side fully hydrogenated. It is experimentally fabricated by removing the hydrogen on one side from graphene, the fully hydrogenated graphene that has hydrogen on both sides. If we score the performance of hydrogenation, graphene, graphone, and graphene are 0, 50, and 100 respectively. By 50% hydrogenation, graphene possesses a small indirect bandgap, which is quite different from both graphene (zero bandgap) and graphane (large direct bandgap), implying potential applications in field-effect transistors, logic devices, and high-speed switching devices, in addition to hydrogen-storage. More importantly, graphene exhibits magnetism and is able to react with electronic and magnetic fields, which is crucially important for applications in nanoelectronics and spintronics. The magnetic moments from unpaired electrons on the unhydrogenated carbon atoms are ferromagnetically coupled, resulting in an infinite magnetic sheet that has homogeneous magnetism in addition to structural integrity in a single layer. Compared to other methods of engineering magnetism, hydrogenation of graphene to graphone is a relatively easy way to obtain magnetism in graphene based nanoelectronics. Furthermore, graphene is thermodynamically stable, which avoids the difficulty of obtaining a magnetic structure through cutting of graphene sheets and thus provides a unique structure for the use of magnetism in nanomaterials. In forming graphone by hydrogenation of graphene on the substrate of hexagonal boron nitride, two great challenging problems (finite band gaps and suitable substrates) are resolved at the same time, holding great promise for advanced post-silicon electronics.

A graphene monolayer could be free-standing, on a substrate, or sandwiched by other layers in real applications. In these cases, it will be strained for two factors as atomic thickness and the presence of strain fields in the environment: for instance, lattice mismatch, surface corrugation of substrates, and spontaneous elastic waves due to vibrations. The strains could profoundly change the properties of graphene monolayers including band structures, magnetism, strengths, and instabilities. Therefore, knowing the elastic properties, including elastic limits and high order elastic constants, is critical in design and practical applications. Particularly, the elastic limit sets the upper boundary of the mechanical load and high order elastic constants describe the non-linear elastic behaviors before material failure. However, it is a great challenge to measure the elastic limits of the graphene monolayers experimentally in addition to its synthesis and manipulation due to the extremely small thickness. To the authors’ best knowledge, there is no experimental report of the structure parameters and elastic properties of graphene. Alternatively, theoretical predictions are also a nontrivial task due to both debonding under extreme loadings and the linkage between

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†Electronic supplementary information (ESI) available: The atomic structural parameters, ultimate stresses and strains, and elastic constants (up to fifth order) are summarized. The calculations use three other exchange–correlation functionals. See DOI: 10.1039/c4nr07665f
atomistic modeling and continuum elastic theory. Here, we report a systematic study on the elastic limits of graphone under mechanical strains using *ab initio* calculations. We find that graphone has a small in-plane stiffness (74%) as well as Poisson ratio (67%) compared to graphene, but similar to those of graphane. These results suggest that hydrogenation reduces the ultimate strength, ultimate strain, and Poisson ratio. In addition, the effect of hydrogenation on the mechanical properties is saturated when the graphene is only 50% hydrogenated.

We use a model of a unit cell consisted of three hydrogen and six carbon atoms, where a periodic boundary condition is applied only along *x* and *y* directions.

First-principles calculations in the frame of Density Functional Theory (DFT) are performed with the VASP code, with the employment of projector augmented wave potentials where carbon’s 2s2 2p2 electrons and hydrogen’s 1s2 electrons are treated as valence electrons. The exchange–correlation functionals are parameterized by Perdew, Burke, and Ernzerhof. We perform all the plane-wave DFT calculations with a kinetic-energy cutoff of 600 eV and a Gamma-centered 24 × 24 × 1 k-mesh. After the structures are relaxed, the forces on each atom are smaller than 0.001 eV Å\(^{-1}\). We set a vacuum region with a thickness of 20 Å in our model to reduce interactions between layers. However, such a vacuum region is user-defined, which may affect the Cauchy stresses calculated for the whole simulation box. Therefore, the second Piola–Kirchhoff (P–K) stress is calculated to straighten out the ill-defined out-of-plane thickness of the monolayers.

Lagrangian strain measures are used to capture the large deformation process. The three independent deformation models are necessary because they provide five stress–strain curves to compute the 14 independent components of elastic constants up to fifth order.

The stress–strain relationship is a unique characteristic of a material, like a “finger-print”. The elastic limits of this material can then be directly read from the stress–strain curves of tensile tests, where the maxima in stresses defines the ultimate stress. The corresponding strain to the ultimate stress is the ultimate strain. Graphone possesses a graphene-like honeycomb structure where there are two typical directions named “armchair” and “zigzag”, as depicted in Fig. 1 together with the geometry of its ground state (the structure parameters are in Table S1 in the ESI†). Strain UNS from –0.1 to 0.4, with an increment of 0.01 for each of the three deformation modes examined in this work. Two of them are uniaxial deformations: one along the armchair direction and the other along the zigzag directions. The last is the biaxial deformation (equally deformed in both directions). The stress–strain relationships of graphone are shown in Fig. 2 compared with graphene and graphane. The strain limits of the armchair, zigzag, and biaxial deformations are 0.16, 0.21, and 0.22, respectively, and the stress limits are 19.8, 22.2, and 22.8 N m\(^{-1}\) respectively.

Graphone behaves asymmetrically in response to compressive (negative) and tensile (positive) strains. The systems under strains larger than the ultimate strain are unstable. They will not exist once perturbations are presented, including defects and thermodynamic motions. The ultimate strain measures the flexibility, which is correlated to the bond strengths. In addition, the ultimate strain is a lower limit of the critical strain, which provides a guide to strain-engineering as well as its various strain-related applications. The ultimate strengths as well as ultimate strains of the three deformation modes are summarized in Table S2 in the ESI†.

The elastic constants are the generalized “strength” of a material as derivatives of the stress–strain curves. Our results of the elastic constants from DFT calculations (ESI Table S3†) supply accurate parameters describing the elastic properties of graphone, which benefits the finite element modeling of graphone at the continuum level. The in-plane stiffness *Y*\(_x\) as well as Poisson’s ratio *ν* are computed from the second order elastic constants *C*\(_{11}\) and *C*\(_{12}\) through the relationships of *Y*\(_x\) = (*C*\(_{11}\) – *C*\(_{12}\))/*C*\(_{11}\) and *ν* = *C*\(_{12}\)/*C*\(_{11}\). The in-plane stiffness of Graphone’s *Y*\(_x\) = 251.7 N m\(^{-1}\) is much smaller than that of graphene (340.8 N m\(^{-1}\)), which implies that the introduced hydrogen decreases the stiffness of graphene. The mechanism of such a reduction in stiffness could be due to the change in bonding characters caused by hydrogenation. For instance, the carbon–carbon bond in graphene (1.48 Å) is 4.4% longer than that in graphene which is 1.42 Å. Effectively, the carbon–carbon bonds in graphene are stretched and, as a result, weakened by hydrogenation. For the same reason, a similar reduction was also observed in graphane.

Besides the in-plane stiffness, the hydrogenation also reduces the Poisson’s ratio by a factor of 1/3 from graphene to graphone. The introduced hydrogen atoms form stiff carbon–hydrogen bonds which are perpendicular to the plane consisting of carbon atoms. These additional carbon–hydrogen bonds enhance the bending modes which involve the C–C–C angles, resulting in a low Poisson ratio. Such a reduction is also observed in other materials with stiff arms including graphane. Compared to graphene, the elastic constants,
bond lengths, in-plane stiffness, and Poisson ratio do not have many differences, as opposed to large differences between graphene and graphone, which indicates that the semi-hydrogenation of graphene already saturates the hydrogenation effect on mechanical strength.

Due to the extremely small thickness, the graphene monolayer is vulnerable to large strains where nonlinear elasticity is prominent. The high-order elastic constants are necessary to describe the nonlinear elastic behaviors, which for example, could be useful in strain-engineering nano-devices. Their importance could be demonstrated by their accuracy in modeling nonlinear elastic behaviors. Take the biaxial deformations in graphone as an example. We plot four stress–strain behaviors, which are predicted from the second, third, fourth, and fifth order elastic constants, respectively, compared with the stress–strain curve from DFT calculations (Fig. 3). We find that the linear behaviors predicted from the second order elastic constants are accurate only up to 0.02. Moreover, the third and fourth order elastic constants are accurate up to 0.07 and 0.14, respectively. For an accurate modeling of the stress–strain behaviors up to its elastic limits, the fifth order elastic constants are indispensable. Similar results are obtained in uniaxial deformations. Such accurately determined strain range is commonly observed in 2D materials.30–32 Furthermore, with these elastic constants, any elastic behaviors can be modeled according to elastic theory.25

Like strains, pressure engineering is also a “clean approach” to tailor the functions and properties by mechanical load without introducing alien species.18 The Poisson ratio is the ratio between transverse and longitudinal strain, which
describes a material’s resistance to distortion rather than to change in volume under strains, providing a universal way to contrast the structural performance of a material.\textsuperscript{29} For a general two-dimensional structure, there is a general trend that the Poisson ratio decreases with an increasing in-plane pressure. The mechanism of such a behavior is that the two-dimensional materials are more easily compressed than sheared under a higher pressure. In other words, the normal modes are more sensitive than shear modes. Contrary to this general trend, the Poisson ratio of graphene increases with an increasing in-plane pressure, as shown in Fig. 4, compared to graphene,\textsuperscript{26} graphite,\textsuperscript{26} h-BN monolayer,\textsuperscript{25} silicene,\textsuperscript{33} and MoS\textsubscript{2} monolayers.\textsuperscript{34} Such a behavior was also observed in calculations with different exchange–correlation functionals (Fig. S1 in the ESI\textsuperscript{†}). This peculiar pressure effect on the Poisson ratio of graphene indicates that the atomic structure of graphene under a higher pressure has a larger tendency to be sheared instead of being compressed. Such a tendency to shear could be an outcome of its atomic structure which has all carbon–hydrogen bonds on one side, lacking the symmetry to balance the shear mode. The reduced symmetry breaks the inversion symmetry. Such an imbalance is a cause of magnetism\textsuperscript{15} as well as spin–orbit band splittings.\textsuperscript{5}

Interestingly, if we regard a graphene monolayer as two opposite balanced graphene monolayers, we can estimate the value of the Poisson ratio of graphene to be half of that of graphene, which is evidenced by the DFT calculations. Our results suggest a practical way to precisely modulate the structural evolution of nanomaterials under mechanical loads by chemical functionalizations including hydrogenation according to symmetry. Furthermore, we tested the case that all hydrogen atoms of graphene are moved to the same side of carbons, as single-side-hydrogenated graphene.\textsuperscript{45} We found the same trend that the Poisson ratio increases with increasing in-plane pressure in this asymmetric structure, which strongly supports our conclusions.

When the strain increases, the stress increases as shown in Fig. 2, leading to a decrement of pressure. As a consequence, the Poisson ratio decrease, which means that the shear strain decreases, to cause the damping of the strain. As a striking consequence, our finding could lead to a new nanodevice – we named it nano strain damper – to keep unpredictable and harmful strains away, ensuring the stable performance of a working nanodevice. By precisely controlled hydrogenation, a graphene-like strip can be formed around the target graphene-based devices as a damper to reduce the collateral shear strains from other parts of graphene substrates or all-graphene electronics.\textsuperscript{16}

It is worthy noting that due to limitation of small unit cell and zero temperature, our DFT model can not capture the out-of-plane ripples, which is another important and interesting topic although has little effect on the in-plane stiffness. As temperature rises, the additional thermal stresses will enhance the shear over compression, resulting in larger strain-damping.

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